

31 May 2001 - Zita
Universe box 28.2

Planck time is as far back as we
can see & make sense of

Particle (e.g. black hole model for pre-big-bang state)

p. 704 "typically cannot be precisely located within
a distance $\lambda_c = \frac{h}{mc}$ " from $\left(\begin{matrix} E = hc \\ \text{wave } \lambda \end{matrix}\right) = \left(\begin{matrix} E = mc^2 \\ \text{particle} \end{matrix}\right)$

Solve for λ :

Event horizon of black hole $D = \frac{2GM}{c^2}$ from
escape velocity: kinetic energy = gravitational energy
 $\frac{1}{2}mv^2 = \frac{GMm}{D}$ let $v = c$

Solve for D :

The smallest black hole that makes sense ($D \geq \lambda_c$)
has a mass $m_p = \text{Planck mass} = \sqrt{\frac{hc^3}{G}} = 5.5 \times 10^{-8} \text{ kg}$

Let $D = \lambda_c$, solve for m_p :

The corresponding size (smallest universe state we
can make sense of) has $\lambda_p = \sqrt{\frac{Gh}{c^3}} = \text{Planck length}$
Sub m_p into D : $\approx 4 \times 10^{-35} \text{ m}$

Earliest time we can make sense of: $t_p = \frac{\lambda_p}{c} = \sqrt{\frac{Gh}{c^5}}$
 $t_p \approx 10^{-43} \text{ s}$