

1. The force of air resistance  $F$  on a falling body can be modeled as depending on the density  $\rho$  the surface area  $A$  and the speed  $v$ . Suppose the relationship is

$$F = k\rho^x A^y v^z ,$$

where  $k$  is a dimensionless proportionality constant and  $x$ ,  $y$  and  $z$  are exponents. Use dimensional analysis to determine the coefficients  $x$ ,  $y$  and  $z$ . [ Note the units of force are  $\text{kg}\cdot\text{m}/\text{s}^2$  and the units of density are  $\text{kg}/\text{m}^3$  ].

2. There are three fundamental constants in physics that involve dimensions of mass, length and time. They are the speed of light  $c = 3.00 \times 10^8 \text{ m/s}$ , which governs the behaviour of objects which go very fast, Plank's constant  $h = 6.63 \times 10^{-34} \text{ kg}\cdot\text{m}^2/\text{s}$ , which governs the behaviour of objects that are very small, and the universal gravitational constant  $G = 6.67 \times 10^{-11} \text{ m}^3/(\text{s}^2\cdot\text{kg})$  which governs the strength of the gravitational interaction between two bodies.

Suppose we could define a length scale  $L$  that depends  $c$ ,  $h$ , and  $G$  in the following way

$$L = c^x h^y G^z$$

Using dimensional analysis find the exponents  $x$ ,  $y$  and  $z$  so that  $L$  has dimensions of length. Then evaluate  $L$  given the values for  $c$ ,  $h$ , and  $G$ . This tiny length scale is called the Planck Length and is believed to be the sized of superstrings which are proposed as the fundamental constituents of matter.