Mathematical Origins of Life

Dancing Patches

In last week's lab we modeled the interaction and growth of a mobile species by making use of NetLogo's breeds. We observed that when interactions were no longer purely random population growth curves were quantitatively different from the predictions of the logistic equation. Indeed when sources and sinks of energy were included, oscillations in population were observed. A common feature of all these models, was that the agents (ie the amoeba and the food) were mobile. It is often the case, in both biology and chemistry that interactions take place between stationary agents. Examples include growth of forests, the growth of algae, or the interactions between cells in an organism. In this lab we will use NetLogo to model such interactions using patches. We will see that although the patches themselves do not move, waves of changes within the patches can mimic various types of complex movement. It is believed that such interactions are responsible for the complex patterns we see in animal coats, and perhaps at a more fundamental level for cell differentiation of a developing embryo.

The Game of Life

The mathematical concept behind the model we will build is that of a cellular automata. The fundamental idea is that each patch can have a number of different states and it changes states by examining the states of its neighbors and following some simple rules. We will start with the well known example of Conway's Game of Life, and build from this to create a somewhat realistic model of the growth of stationary species. The model can be extended readily to include the sorts of chemical reactions that play a role in animal development.

In the Game of Life, patches can have two states: alive and dead. A patch which is dead will come to life in the next generation if it has three live neighbors. A patch that is alive will only continue to live if it has either two or three live neighbors. In this model we will let a patch that is alive have the state 1 and a patch that is dead have the state 0.

Start your model by writing defining the state variable for the patches: patches-own [state]

Then write a procedure called random-setup which randomly assigns either a 0 or a 1 the sate variable of each patch and then colors patches that have state 1 white and those with state 0 black. An efficient way of doing this is

```
to random-setup
ca
ask patches [
set state random 2
set pcolor scale-color red state 0 1
]
end
```

The line in which the pcolor is defined may seem funny (especially the red part!), but make sure you understand how it works, and check that it does work by creating a button to use the procedure and check that white patches do indeed have state 1 and black patches have state 0. There are certainly other ways of doing this, but this one will generalize naturally to the extensions you will do for homework.

Rules of the Game

Now it is time to apply the cellular automata rules for the Game of Life

We will do this in a go procedure. The only thing this procedure needs to do is change the state of a patch according to the rules of the Game of Life. However, there is one subtlety you should be aware of. Since NetLogo executes commands to different patches sequentially if you are not careful one patch may change its state, before its neighbor has had a chance to ask it what state it was in. In order to keep all changes in step, we will first ask each patch to keep a record of the total number of its neighbors that are alive (state 1). Only once all of the patches have done this will we allow them to change state. The rule to change the state can be applied efficiently by using the an *ifelse* statement which allows you to execute different commands when different conditions apply. Nested *if* statements are used when more than two conditions apply

```
to go
    ask patches [set total count neighbors with [state = 1]]
    ask patches [
        ifelse total = 3
        [set state 1]
        [if total !=2 [set state 0] ]
        set pcolor scale-color red state 0 1
   ]
end
```

In order for the above code to be complete you need to add the variable total to the patches-own list. Notice the use of the neighbors primitive. This returns a list of the 8 patches surrounding the patch in question. Make sure you follow the logic of the if statement in this procedure. Later you may want to change the rules to create your own cellular automata. Create a button for the go procedure and test it.

Designing Life

After some initial craziness you should see the patches settle down to a few simple stable structures and perhaps a few blinking patterns. It may not appear too "life"-like but in fact there are a whole host of interesting "organisms" in the Game of Life, some of which appear to move (gliders), others which breed (breeders). If you run your game a few times you might see a few of these emerge. To see the more complicated "organisms" you need build them. There is no blind watchmaker in the Game of Life. Although it has been shown that it is theoretically possible to create self replicating "molecules" á la DNA these are not stable to invasion by "parasites" and have no hope of evolving. However, we can be "watchmakers" by drawing "organisms" on a blank canvas. We can do this by using NetLogo's ability to track the location of the mouse.

First create a blank-slate procedure that sets all the patches to be dead

```
to blank-slate
ca
ask patches [
set state 0
set pcolor black
]
end
```

Now create a new procedure that will turn the patch at the location of the mouse to be alive

(white and state 0) when the mouse is pressed

```
to draw

if mouse-down? [

ask patch at mouse-xcor mouse-ycor [

set state 1

set pcolor white

]

]

end
```

Since it is likely you will also want to erase mistakes, create a similar procedure called erase to that you can use to "kill" a patch. The draw and erase procedures should be executed with "run forever" buttons. You may find it useful to put a command in your go procedure to stop if the mouse is down.

Play around with this code for a while and see what lifeforms you can create. I'll have a few suggestions for you to look at. At this time you may want to try modifying the rules of the game in some way to see what other "lifescapes" you can create.

Homework

Although the "organisms" you created in the Game of Life may mimic biology, they are not a biological model per se. However, we can easily modify the code to model different models in biology and chemistry. Here is what I propose, Let's allow the state variable in the above program to be the age of some organism. (I suggest you relabel it as age to make this explicit in your code). We will have patches get older each year until they reach a maximum age, at which point they are considered dead (and we set their age to 0). Patches will only die by reaching old age. Let's have a model where new cells can only be born in patches that are dead and which also have the exactly the right number of fertile neighbors. We could call these fertile neighbors parents.

- 1. First rescale your screen to be 50 by 50 with patch size 5
- 2. Let the age variable range from 0 to max-age. Were max-age can be specified by a slider (choose a slider range for max-age to be 1 to 100).
- 3. Since we have cells ranging in ages from 0 to max-age, modify your random-setup procedure to create patches of all ages. Also make sure you you change your scale-color range to include the full spectrum of ages.
- 4. Now modify the rules. As first rule let the age at which our organisms reach fertility be 15 and the age at which they become sterile be 50. Let the number of parents that are needed for a dead cell to be reborn be 2.
 - (a) Change your go procedure so that total is the number of fertile neighboring patches.
 - (b)Modify the next part of your go procedure to ask the patches which are not dead to get older by one year and then if their age is greater than the maximum age to die. For those that are already dead (age 0) ask them to be reborn if they have exactly 2 parents.
 (c)Make sure your command to color the patches is scaled correctly.
- 5. Run your modified program. Experiment with different values for max-age to see how having non-reproductive neighbors affects the population distribution.
- 6. Modify your program so that you have sliders ranging from 0 to 100 for both the fertileage and the sterile-age. Also add a slider from 0 to 8 for parent-number. Modify the appropriate lines in your program.
- 7. Add commands that will allow you to plot the total number of patches in each age group: immature, fertile, and sterile.

- 8. Now explore your model in detail. Experiment by starting with a random initial distribution of ages and with a blank-slate on which you seed your own pattern of newborn patches. You will find that some behavior can only be obtained by carefully tuning the sliders as the model runs.
- 9. With max-age set at 100 and parent-number set at 2 find parameter values for fertile-age and the sterile-age for which each of the following types of patterns:
 - (a) The population exists only in isolated groups that appear to drift across the screen.
 - (b)The changing population distribution appears to move in large lacey waves across the screen.
 - (c)The changing population distribution resembles a tight spiraling pattern.
 - (d)The population appears to change in a random way.
 - (e)The majority of patches appear to change together in a synchronized way.
 - Write your values and descriptions in the information section of your Netlogo program
- 10.Try to get qualitatively different patterns using different values for max-age and parentnumber. In particular, try getting "Life" like patterns with low values for max-age. Also try setting parent-number to 0. You might also want to consider modifying your code to allow for a range of acceptable neighboring parents for rebirth to take place (eg 2 or more parents would be a suitable model for some fruit trees).
- 11. The above patterns are observable in nature for systems which grow in the way described. It is straight forward to change the code to model a reaction-diffusion type chemical process like the B-Z reaction. To do this we let the age represent the concentration of some chemical. During each time step the concentration can change in following ways:
 - (a) First it can increase by a constant amount due to the presence of some precursor chemical which is in large supply. (This is the *reaction* part of chemical process and is similar to how we change age in the biological model we just made, accept it can increment by more than one each time step).
 - (b)Second, it can increase by adding some fraction of the total concentration of its neighbors to its own total. (this is the diffusion part of the chemical process and is similar to counting parents in the biological model accept here we total the concentration, rather than the number of parents, and all patches can increase there concentration by diffusion).
 - (c)Finally the concentration is reset to zero when it gets too high (this is the inhibition part of the chemical process. This is akin to dying in our model).

This question is optional, but it is worth making it work if you can since it leads to remarkable patterns that differ from the ones you created in the biological model above.

12.Save your lab 4model, giving it the name "lastname_firstname_week_4.nlogo". When you are finished the homework drop this file in the dropbox folder. Before submitting your NetLogo program write comments for all your procedures explaining what each "non obvious" line does.