

Physics of Astronomy - module 7 - Grancoli Ch 7 & 8  
Phys A

work & Energy

E7.2

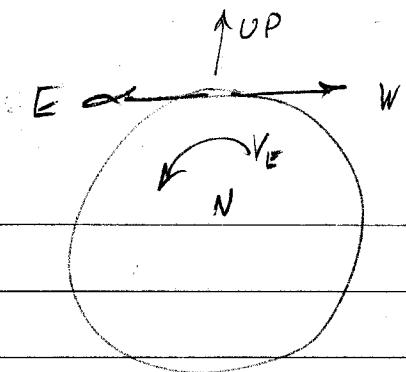
Ch 7 # 4, 6, 21, 34, 39, 41, 52 / Ch 8 # 10, 32, 45, 47

4. (I) A 1200-N crate rests on the floor. How much work is required to move it at constant speed (a) 4.0 m along the floor against a friction force of 230 N, and (b) 4.0 m vertically?

6. (I) How high will a 1.85-kg rock go if thrown straight up by someone who does 80.0 J of work on it? Neglect air resistance.

Q8\*

45. (II) Take into account the Earth's rotational sp (1 rev/day) and determine the necessary speed, with res to Earth, for a rocket to escape if fired from the Earth at equator in a direction (a) eastward; (b) westward; (c) vertically upward.



Sun rises east  $\rightarrow$  west

So Earth turns west  $\rightarrow$  east

What is the speed of the earth at the equator?

$$V_{\text{EARTH}} = V = \frac{2\pi R}{T} =$$

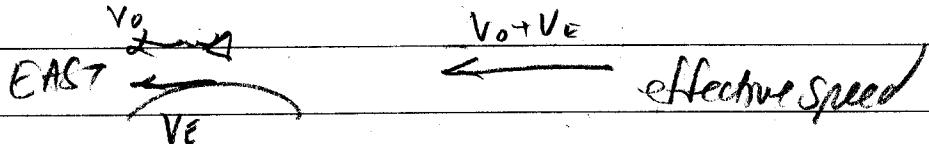
What is the escape speed, ignoring Earth's motion?

Last week we derived this:  $K = U$

$$\frac{1}{2} m V_e^2 = \frac{GMm}{R}$$

$$V_{\text{escape}} = V_e =$$

- (a) Consider a rocket fired EASTward with a speed  $V_0$  RELATIVE to Earth. It's like throwing a ball out a car window; the ball goes faster if the car is moving.



$$V_{\text{escape}} = V_e = V_0 + V_E \rightarrow \text{Solve for } V_0 = \text{rocket speed.}$$

45(b) Consider a rocket launched WESTWARD

$$V_o \rightarrow$$

The rocket must overcome Earth's motion  $V_E$

$$V_{\text{esape}} = V_o - V_E \rightarrow \text{Solve for } V_o$$

(c) Consider a rocket launched UP

$$V_{\text{esc}}$$

$$V_{\text{esape}}^2 = V_E^2 + V_o^2. \text{ Solve for } V_o.$$

$$\uparrow V_o$$

$$\leftarrow V_E$$

Re-denote escape speed:

47. (II) (a) Determine the rate at which the escape velocity from the Earth changes with height above the Earth's surface,  $dv_{\text{esc}}/dr$ . (b) Use the approximation  $\Delta v \approx (dv/dr) \Delta r$  to determine the escape velocity for a spacecraft orbiting the Earth at a height of 300 km.

$$K = U$$

$$\frac{1}{2}mv_e^2 = \frac{GMm}{r}$$

$$V_e =$$

In general, at some distance  $r$  from Earth's center

$$V_e(r) =$$

(a)  $\frac{dV_e}{dr} =$

- (b) We know from #45 that  $V_e =$   
at Earth's surface ( $r = R_E$ ). Above the surface  
 $V(r) \approx V_e + \Delta V$  where  $\Delta V \approx \frac{dV_e}{dr}$

At a height of  $\Delta r = 300 \text{ km}$ ,  $\Delta V =$

Then  $V(300 \text{ km}) =$