

Day 5 of Astro. winter wk 3

ZITA  
22 Jan 06

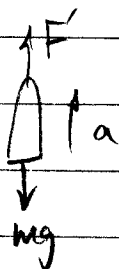
Ch 4 #5, 21, 34, 40, 72, 55

21. (II) A Saturn V rocket has a mass of  $2.75 \times 10^6$  kg and  $F$  exerts a force of  $33 \times 10^6$  N on the gases it expels. Determine (a) the initial vertical acceleration of the rocket, (b) its velocity after 8.0 s, and (c) how long it takes to reach an altitude of 9500 m. Ignore the mass of gas expelled (not realistic) and assume  $g$  remains constant.

$$F = ma'$$

$$(a) a' = \frac{F'}{m} = \frac{33 \times 10^6 \text{ N}}{2.75 \times 10^6 \text{ kg}}$$

$$a' = \frac{3 \cdot 11}{2 \cdot 75} = 3.4 = 12 \left( \frac{\text{kg}}{\text{kg}} = \frac{\text{m}}{\text{s}^2} \right) = \text{thrust acceleration}$$



Note that the rocket needs an <sup>upward</sup> acceleration of  $g$  just to LEVITATE. So only part of  $a'$  contributes to the upward acceleration  $a$ .

$$\sum F = F' - mg = ma$$

↑ thrust    ↑ weight    ↑ actual upward accel.

$$a = \frac{F' - mg}{m} = \frac{F'}{m} - g = a' - g = 12 \frac{\text{m}}{\text{s}^2} - 9.8 \frac{\text{m}}{\text{s}^2} = 2.2 \frac{\text{m}}{\text{s}^2}$$

After 8 sec:

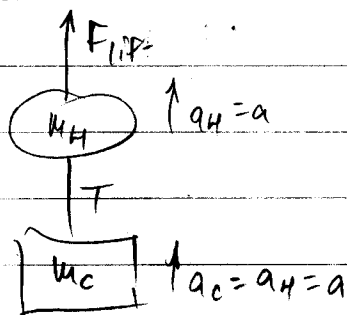
$$(b) v = v_0 + at = 0 + at = 2.2 \frac{\text{m}}{\text{s}^2} (8 \text{ s}) = \frac{\text{m}}{\text{s}}$$

$$(c) \text{ Time to reach } x = 9500 \text{ m? } x = \frac{1}{2}at^2 = v_0 t + x_0$$

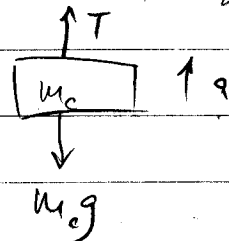
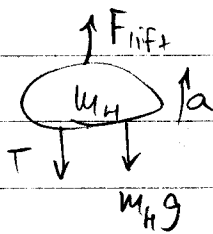
$$t = \sqrt{\frac{2x}{a}} = \sqrt{\frac{2 \cdot 9500 \text{ m}}{2.2 \frac{\text{m}}{\text{s}^2}}} = \text{---}$$

34. (II) A 7500-kg helicopter accelerates upward at  $0.52 \text{ m/s}^2$  while lifting a 1200-kg car. (a) What is the lift force exerted by the air on the rotors? (b) What is the tension in the cable (ignore its mass) that connects the car to the helicopter?

If the rope isn't stretching, then  $a_H = a_c = a$



Draw separate free-body diagrams



$$\sum F = ma : m_H a = F_{\text{lift}} - T - m_H g, \quad m_c a = T - m_c g$$

Two equations in two unknowns. Solve for  $T$  and  $F_{\text{lift}}$

① Eliminate  $T = F_{\text{lift}} - m_H g - m_H a$

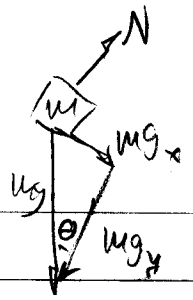
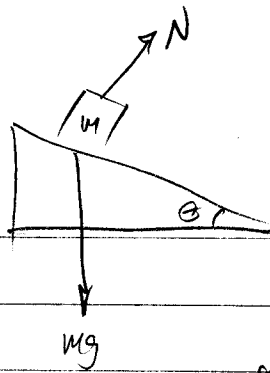
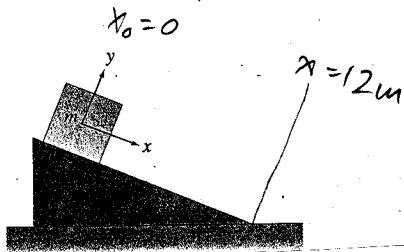
②  $T = m_c a + m_c g$

$$F_{\text{lift}} - m_H (g + a) = m_c (a + g)$$

$$\text{Solve for } F_{\text{lift}} = (m_c + m_H)(a + g) =$$

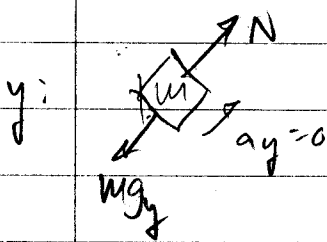
We could sub  $F_{\text{lift}}$  into Eqn ① to find  $T$ , but we already have ②:  $T = m_c (a + g) =$

40. (II) The block shown in Fig. 4-44 has mass  $m = 7.0 \text{ kg}$  and lies on a smooth frictionless plane tilted at an angle  $\theta = 22.0^\circ$  to the horizontal. (a) Determine the acceleration of the block as it slides down the plane. (b) If the block starts from rest  $12.0 \text{ m}$  up the plane from its base, what will be the block's speed when it reaches the bottom of the incline?



$$mg_x = mg \sin \theta$$

$$mg_y = mg \cos \theta$$

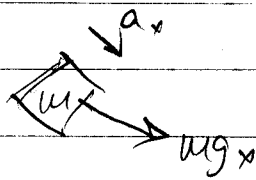


Draw a free body diagram for each direction

$$\sum F_y = ma_y$$

Block is not jumping up off the incline or falling through it, so  $a_y = 0$

$$N - mg_y = ma_y = 0$$

$$N = mg_y = mg \cos \theta$$


In the absence of friction,

$$\sum F_x = ma_x = mg_x$$

So  $a = a_x = g_x = g \sin \theta$

$$a = 9.8 \frac{\text{m}}{\text{s}^2} \sin 22^\circ = \frac{\text{m}}{\text{s}^2}$$

(b)  $x(t) = x_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow$  time to reach bottom is

$$t = \sqrt{\frac{2x}{a}}$$

Speed at bottom:  $v(t) = v_0 + at = at = a \sqrt{\frac{2x}{a}} = \sqrt{2xa}$

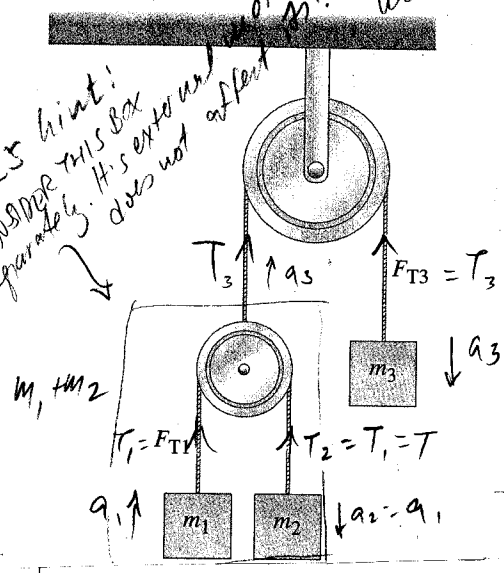
You could get the same answer by solving  $v^2 - v_0^2 = 2ax$

$$v(t) = \sqrt{2xa} = \sqrt{2(12\text{m})\left(\frac{\text{m}}{\text{s}^2}\right)} = \frac{\text{m}}{\text{s}}$$

Let arrows indicate directions. Avoid  $\ominus$  signs.

55. (III) The double Atwood machine shown in Fig. 4-52 has frictionless, massless pulleys and cords. Determine (a) the acceleration of masses  $m_1$ ,  $m_2$ , and  $m_3$ , and (b) the tensions  $F_{T1}$  and  $F_{T3}$  in the cords.

Pulleys hint:  
CONSIDER THIS BOX  
Separately. It's external motion does not affect internal motion.

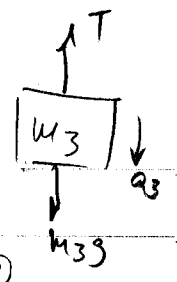


$$\sum F_3 = m_3 a_3$$

$$\downarrow \sum F_3 = m_3 g - T_3$$

$$m_3 a_3 = m_3 g - T_3$$

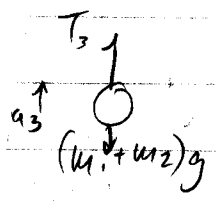
①



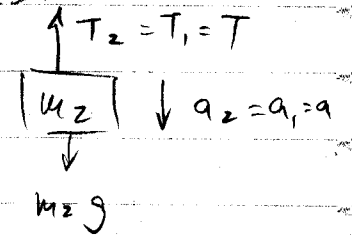
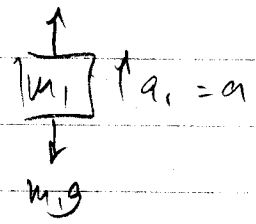
$$\uparrow \sum F = ma$$

$$T_3 - (m_1 + m_2)g = (m_1 + m_2)a_3$$

②



$$T_1 = T \text{ (INSIDE THE BOX)}$$



$$\sum F_1 = m_1 a_1$$

$$T - m_1 g = m_1 a$$

$$\sum F_2 = m_2 a_2$$

$$m_2 g - T = m_2 a$$

Ch 4

The easiest problem:

- (5.) What is the weight of a 58-kg astronaut (a) on Earth, (b) on the Moon ( $g = 1.7 \text{ m/s}^2$ ), (c) on Mars ( $g = 3.7 \text{ m/s}^2$ ), (d) in outer space traveling with constant velocity?

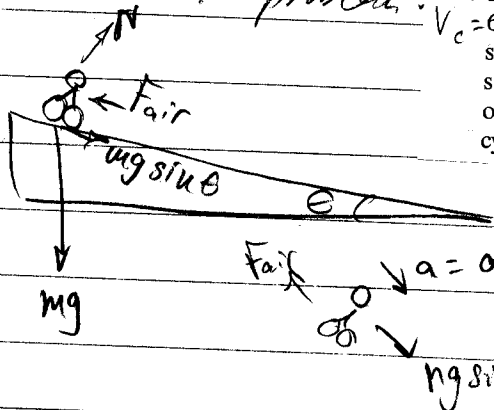
Weight =  $mg$  depends on local gravity, though the astronaut's mass DOES NOT CHANGE

(a) on Earth,  $W_{\text{Earth}} = 58 \text{ kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} = \underline{\hspace{2cm}} \text{ N}$

(b) on Moon,  $W_{\text{Moon}} = 58 \text{ kg} \cdot 1.7 \frac{\text{m}}{\text{s}^2} = \frac{1}{6} W_E = \underline{\hspace{2cm}} \text{ N}$

(c) on Mars,  $W_{\text{Mars}} = 58 \text{ kg} \cdot 3.7 \frac{\text{m}}{\text{s}^2} = \underline{\hspace{2cm}} \text{ N}$

The hardest problem?



72. A bicyclist can coast down a  $5.0^\circ$  hill at a constant speed of  $v_c = 6.0 \text{ km/h}$ . If the force of air resistance is proportional to the speed  $v$  so that  $F_{\text{air}} = cv$ , calculate (a) the value of the constant  $c$ , and (b) the average force that must be applied in order to descend the hill at  $20.0 \text{ km/h}$ . The mass of the cyclist plus bicycle is  $80.0 \text{ kg}$ .

COASTING: SPEED = CONSTANT

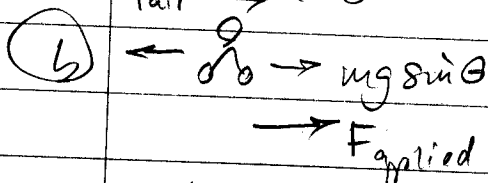
$$\frac{dv}{dt} = 0 = a$$

$$\sum F = ma = 0$$

$$F_{\text{air}} - mg \sin \theta = 0$$

$$cv = mg \sin \theta$$

(a)  $c = \frac{mg \sin \theta}{v} = \frac{80 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot \sin 5^\circ}{6.0 \cdot 10^3 \frac{\text{m}}{\text{hr}} \cdot \frac{1 \text{ hr}}{3.6 \cdot 10^3 \text{ s}}} = \underline{\hspace{2cm}} \frac{\text{kg}}{\text{s}}$



$$\sum F = 0 = F_{\text{applied}} + mg \sin \theta - F_{\text{air}}$$

$$F_{\text{applied}} = F_{\text{air}} - mg \sin \theta$$

$$v' = 20 \frac{\text{km}}{\text{hr}} \cdot \frac{10^3 \text{ m}}{1 \text{ km}} \cdot \frac{1 \text{ hr}}{3.6 \cdot 10^3 \text{ s}} = \underline{\hspace{2cm}} \frac{\text{m}}{\text{s}}$$

$$F_{\text{applied}} = cv' - mg \sin \theta = \underline{\hspace{2cm}} \text{ N}$$

# Physics of Star Trek ROCKET PROBLEM

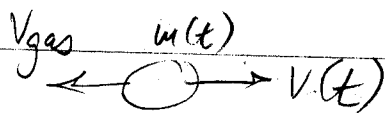
p. 25 - "To accelerate to half the speed of light, The Enterprise must burn 81 times its entire mass in Hydrogen fuel" (1% of which streams out as He atoms after fusion)

$$V_{\text{final}} = \frac{c}{2} \quad M_0 = \text{ENTREPRISE MASS + FUEL INITIALLY}$$

$$V_{\text{exhaust gas}} = \frac{c}{8} \text{ (relative to rocket)}$$

$$\text{Show that } M_0 = 81 M_{\text{final}} = 81 M_{\text{ship}}$$

First try it NONRELATIVISTICALLY (too simple) as in Ex 9-18 on Giancoli p. 279



$$F_{\text{thrust}} = v_{\text{gas}} \frac{dm}{dt}$$

We'll ignore initial acceleration  $a$  to overcome gravity - assume we're out in space.

$$(F = ma \text{ is, more generally, } F = \frac{d}{dt} m v = m \frac{dv}{dt} + v \frac{dm}{dt})$$

$$\text{Momentum conservation: } -m \frac{dv}{dt} = v_{\text{gas}} \frac{dm}{dt}$$

$$-m dv = v_{\text{gas}} dm$$

$$-dv = \frac{dm}{m} \frac{v_{\text{gas}}}{v}$$

$$\int_{t=0}^t \frac{1}{v_{\text{gas}}} dv = \int_{v_0}^{v(t)} \frac{1}{v_{\text{gas}}} (v_{\text{gas}} - v_0) = \frac{v_{\text{final}}}{v_{\text{gas}}} = - \int \frac{dm}{m} =$$