## Atoms, Molecules \& Reactions, Spring 2006

## Quantum Mechanics Homework

1. Generate the following two equations using $\frac{\partial E}{\partial C_{1}}=0$ and $\frac{\partial E}{\partial C_{2}}=0$
$\mathrm{C}_{1}\left(\mathrm{H}_{\mathrm{AA}}-\mathrm{E}\right)+\mathrm{C}_{2}\left(\mathrm{H}_{\mathrm{AB}}-\mathrm{ES}\right)=0 \quad$ Equation 1
$\mathrm{C}_{1}\left(\mathrm{H}_{\mathrm{AB}}-\mathrm{ES}\right)+\mathrm{C}_{2}\left(\mathrm{H}_{\mathrm{AA}}-\mathrm{E}\right)=0 \quad$ Equation 2
2. Substituting the energy values we obtained in class for $\mathrm{H}_{2}{ }^{+}$in the following equations, obtain a relationship between $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$.

$$
\begin{array}{ll}
\mathrm{C}_{1}\left(\mathrm{H}_{\mathrm{AA}}-\mathrm{E}\right)+\mathrm{C}_{2}\left(\mathrm{H}_{\mathrm{AB}}-\mathrm{ES}\right)=0 & \text { Equation } 1 \\
\mathrm{C}_{1}\left(\mathrm{H}_{\mathrm{AB}}-\mathrm{ES}\right)+\mathrm{C}_{2}\left(\mathrm{H}_{\mathrm{AA}}-\mathrm{E}\right)=0 & \text { Equation } 2
\end{array}
$$

3. Using the relationships you obtained in (2) above and the following facts, calculate the values of $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$.
o $\psi=\mathrm{C}_{1} 1 \mathrm{~S}_{\mathrm{A}}+\mathrm{C}_{2} 1 \mathrm{~S}_{\mathrm{B}}$
o The wave function $\psi$ is normalized.
4. Write the complete wave functions you obtained in (3) above. Then draw a rough sketch of these wave functions.
