## Mathematical Origins of Life

#### Biomorphs

In *Climbing Mount Improbable*, the author, Richard Dawkins, discusses how organisms evolve because random mutations in the genotype result in a change in phenotype, which then subject to selection pressure. The set of all possible phenotypes forms a high dimensional phenotype-space and evolution can be viewed as wandering through the various possible phenotypes on a path that increases in fitness. Dawkins creates digital creatures, which he called biomorphs, to illustrate this idea. This what we will do in this lab. We will use NetLogo to build a geometric structure following a simple set of rules. The rules then become a genome for the creatures, which is subject to random mutations from one generation to the next. The selection pressure comes from you. You choose which mutated form to breed and which to let die. In the end you wander through biomorph-space until a pleasing form emerges.

### Making Branching Creatures

The basic form we will choose for our creatures is a branching structure. The main idea is to create a turtle that plays the role of a seed. It produces a bud, which moves forward, with the pen down to draw a stem, this bud then hatches two new buds, and dies. Each new bud then repeats the process a certain number of times until a tree-like structure is formed.

So that we all start with the same code, I've included two procedures that work together to implement this idea below. The first creates the "seed" turtle wherever the mouse is clicked and assigns the seed some parameter values that will determine how it grows. The second procedure makes the seeds grow into a tree-like structure. You will need to create two new breeds (seeds and buds) and make the variables n, step, and angle, into turtles-own variables. Make a go procedure that calls the two procedures below and create a setup procedure that clears the screen. Add a setup and a go button on your interface. Give yourself lots of space by changing the world-view to 100 by 100 with patch size 5.

```
to plant-seeds
if mouse-down? [
     create-seeds 1 [
          setxy mouse-xcor mouse-ycor ; put seed where the mouse is
          set heading 0 ; face the top of the screen
          set n 5
                         ; number of repetitions
          set step 4 ; length of each branch
          set angle 25 ]] ; angle of branching
                          ; wait 0.1 seconds before planting next seed
wait 0.1
end
to grow-seeds
    ask seeds [
        pendown
                         ; get ready to draw the branches
        hatch-buds 1 [] ; make a bud to draw the main stem
        repeat n [
               ask buds [
                                       ;draw the stem
                     fd step
                     hatch 1 [rt angle] ; make a new bud on the right
                     hatch 1 [lt angle] ;make a new bud on the left
                    die ]] ; central bud dies after drawing stem
        ask buds [die] ; branching buds die after drawing branches
                    ; remove seeds so they don't grow again
        die l
end
```

You should get a basic tree structure whenever you click the mouse on the screen. Try changing the values assigned to n, step and angle in the plant-seeds procedure to see how changing the parameters changes the shape of your biomorph. Choosing very large angles make for interesting structures, that don't look much like trees. Play around with these values for a while to see what gives interesting shapes. You could make sliders called n-value, step-value and angle-value corresponding to the values you give these variables. Careful, don't let the n-value slider go higher than 12 or you may crash NetLogo.

With the current set-up you have three variables you can adjust to vary the biomorphs. You can think of these variables as the genes of the creatures, and changing the variables corresponds to moving through three-dimensional biomorph-space.

Now let's try modifying our procedure so that it has a few more genes to vary. One thing we might consider doing is breaking the symmetry of our creatures a little.

### Symmetry breaking

We will keep bilateral symmetry – that is, mirror symmetry on the main axis – but after the first branch we will allow left branch angles to be different from right branch angles. We'll need to keep track of which bud is on the right and which is on the left. First add turtles-own variables called right?, angle-1 and angle-2. Now when you create the seed in your plant-seeds procedure add lines to give values to angle-1 and angle-2 (try 30 and 90). Then modify your grow-seeds procedure so that a seed hatches not one bud, but two buds, one which will have right? set to true and will turn right by an amount angle and the second will have right? set to false and turn left by an amount angle. Do this by replacing the line

hatch-buds 1 []

#### with the lines

Then we want the right bud to make branches that are asymmetrical, and the left bud to make branches that are mirror images of the right branches. So in the repeat command block replace the lines where you ask buds to hatch a new bud on the right and another on the left, with the following lines which hatch buds at different angles depending on whether they are right or left buds.

```
ifelse right?
    [ hatch 1 [rt angle-1]
        hatch 1 [lt angle-2] ]
    [ hatch 1 [lt angle-1]
        hatch 1 [rt angle-2] ]
```

(Note the structure of the *ifelse* command which is followed by a true/ false statement and two command blocks. If the condition is true the first command block is executed and if it is false the second is executed)

You now have increased the number of genes from three to five genes. Try it out using different values for the new variables, you should get some more variety, depending on how large you make angle-1 and angle-2. You could add sliders called angle-1-value and angle-2-value to represent the values you give these variables. This will help you explore the model. We will now add three more genes (variables) to the genome of our creatures. The creature is made by repeating a series of commands inside the repeat command block n times. In an actual tree the branch length (step) decreases in size as you go up the tree. A similar thing happens with the branching angle. Each time we run the commands in the repeat command block lets change the step size and the two angles angle-1 and angle-2 by multiplying by some factor. Add new variables called step-factor, angle-1-factor and angle-2 factor to the turtles-own list and then in your plant-seeds procedure assign values to these variables (try using something like 0.8 for the step-factor and 2 for the angle factors).

Now, inside the repeat command block of your grow-seeds procedure include lines that change step, angle-1 and angle-2 by the appropriate factors. Now see what happens for different values of these factors. You should get interesting creatures – especially if the angle-factors are large. (You get a mess if the step factor is large!).

# Assignment

At the moment you change your creatures by choosing values for the various genes. This is not how evolution does it. For evolution you need variation (different genes for different seeds), selection, mutation and reproduction. We will start by creating nine seeds, each of which is a slightly mutated version of its neighbor and arranging them evenly around the screen. Then we will select the "fittest" creature, and this one will be allowed to reproduce. Its offspring will all be displayed on the screen, each of which will have a slight mutation, and then we select again. By a gradual process of mutation and selection we will see the creatures evolve.

- In your plant-seeds procedure remove all reference to the mouse you will not plant-seeds with the mouse any more. Create 9 seeds instead of 1. After the create-seeds command block call an arrange-seeds procedure. You need to write this procedure to place the seeds (which will have who numbers 0 through 8) evenly around the world. Leave turtle 8 at the center of the screen and then place turtles 0 through 7 in a square around the center using the setxy command. Make good use of space.
- 2. Now we want to give each of the seeds a genome. We can do this by defining a seedsown variable called genome. This will be as a variable that is a list that contains the values you assigned to the different variable names using the sliders. As an example, suppose I only have the variables n, step and step-factor as genes, then I would include the following line as the last entry in the create-seeds command block in the plant-seeds procedure to make my genome list

```
set genome (list n step step-factor)
```

You will have a longer list. At the moment each seed will have the same genome. That will change after we mutate them. (Remember the order of the list. It is important.)

3. In order to allow your seeds to mutate define a globals variable called mutation-rates. This will be a list that defines the increments by which each of the genes can change in each generation. The order of this list should be the same as the order for the genome list. For example if I want n to change by 1, and step to change by 1 and step-factor to change by 0.1 in each generation I would define mutation-rates as follows: set mutation-rates [1 1 0.1]

Add a line like this, with your complete list of mutation rates, to your setup procedure right after you clear-all. When choosing the mutation rates, make sure there is scope for small, but still significant change. Use your earlier experiments to choose sensible values.

4. Now you need a mutate procedure that mutates the genome of turtles 0 through 7. (turtle 8 will be left un-mutated). Since we have 8 genes lets have turtle 0 be the one with gene 0 mutated and turtle 1 have gene 1 mutated and so on. To mutate a gene we have to randomly add or subtract the corresponding value from the mutation-rates list for the gene we want to mutate. The syntax for changing values in lists is a little awkward so I'll include the code for the mutate procedure below. Make sure you understand what each part does. Call the mutate procedure right after arranging the seeds in the plant-seeds procedure. Here is the code:

```
to mutate
  ask seeds with [who < 8 ][
      ifelse (random 2) = 1 ; add the mutation rate if 1 and subtract if 0
      [ set genome replace-item who genome ( (item who genome) + (item who
mutation-rates) )]
      [ if (item who genome) > (item who mutation-rates)
           [ set genome replace-item who genome ( (item who genome) -
           (item who mutation-rates) ) ] ]
      end
```

5. Now that your seeds are planted and mutated they are ready to grow. For the seeds to grow they need to know what the values of their genes are. Although you have given these values to the genome list you haven't yet assigned these values to the variable names you use in your grow-seeds procedure. Define an assign-values procedure where you assign each variable the appropriate value in the genome. For example, if the variable n corresponds to the first entry in the genome list and step was the second value in the genome list then you would have the following lines in the assign-values procedure.

set n (item 0 genome)
set step (item 1 genome)

Note the typical programming convention that the first item in a list is called item 0 and the second item is called item 1. Complete this procedure, and then call it in the plant-seeds procedure immediately after the mutate procedure.

- 6. Now remove calls to plant-seeds and grow-seeds from your go procedure and put them in your setup procedure. When you press setup you should get nine slightly different creatures. It should all work wonderfully now, once you remove any bugs. Actually it would be helpful if you also remove the last die command in your branch procedure, where you removed the seeds. We will want to keep the seeds around for the final part of the program.
- 7. You are nearing the end of this lab. You now need to modify your go procedure so that you can use the mouse to select your favorite creature. Define a new globals variable called fittest at the top of the procedures tab. This variable is the creature we will select with the mouse. In the go procedure include a line that sets fittest to be the seed closest to the mouse whenever it is pressed down. You'll need to use the distancexy reporter and the min-one-of reporter for this. I'll let you look these up in the manual.

- 8. Now in the go procedure, whenever the fittest seed is selected with the mouse have all seeds set their genome to the genome of the fittest seed, then clear the screen of all the drawings (but not the seeds), mutate the seeds, assign-values to their genes and then grow your newly evolved creatures by calling grow-seeds.
- 9. You should now be able to select your favorite turtle with a mouse click. When you do, you should see your selection appear in the middle. If your mutation rates are about right you should be able to weave your way through biomorph-space, selecting creatures without much care for the actual genes. If you want to keep track of the actual gene's you should add monitors showing each of the gene's for turtle 8, who will always be the latest selected.
- 10. Although we have no room left for genes, you might want to change the color of your creatures by linking the color to one of the other genes. For example in the repeat command block you could add a line: set color (angle-1 angle-2) and see what it does (feel free to try other things be creative).
- 11. Now have some fun. Evolve three new creatures, and include the genetic code for these creatures in a note on the interface. Then Save your model, with naming convention "lastname\_firstname\_Lab\_5\_biomorph.nlogo". When you are finished the homework drop this file upload it to our Moodle site. The due date is May 5<sup>th</sup>.